

6.6-6.7] Models of Sinusoidal Functions

creating the equation of $\sin(x)$ and $\cos(x)$

3 ways:

① Graph

② Table

③ Words.

Infinite answers!!!

$a = a$
- amp, period, eqⁿ of axis
is the same

- phase shift is different
 d

Remember:

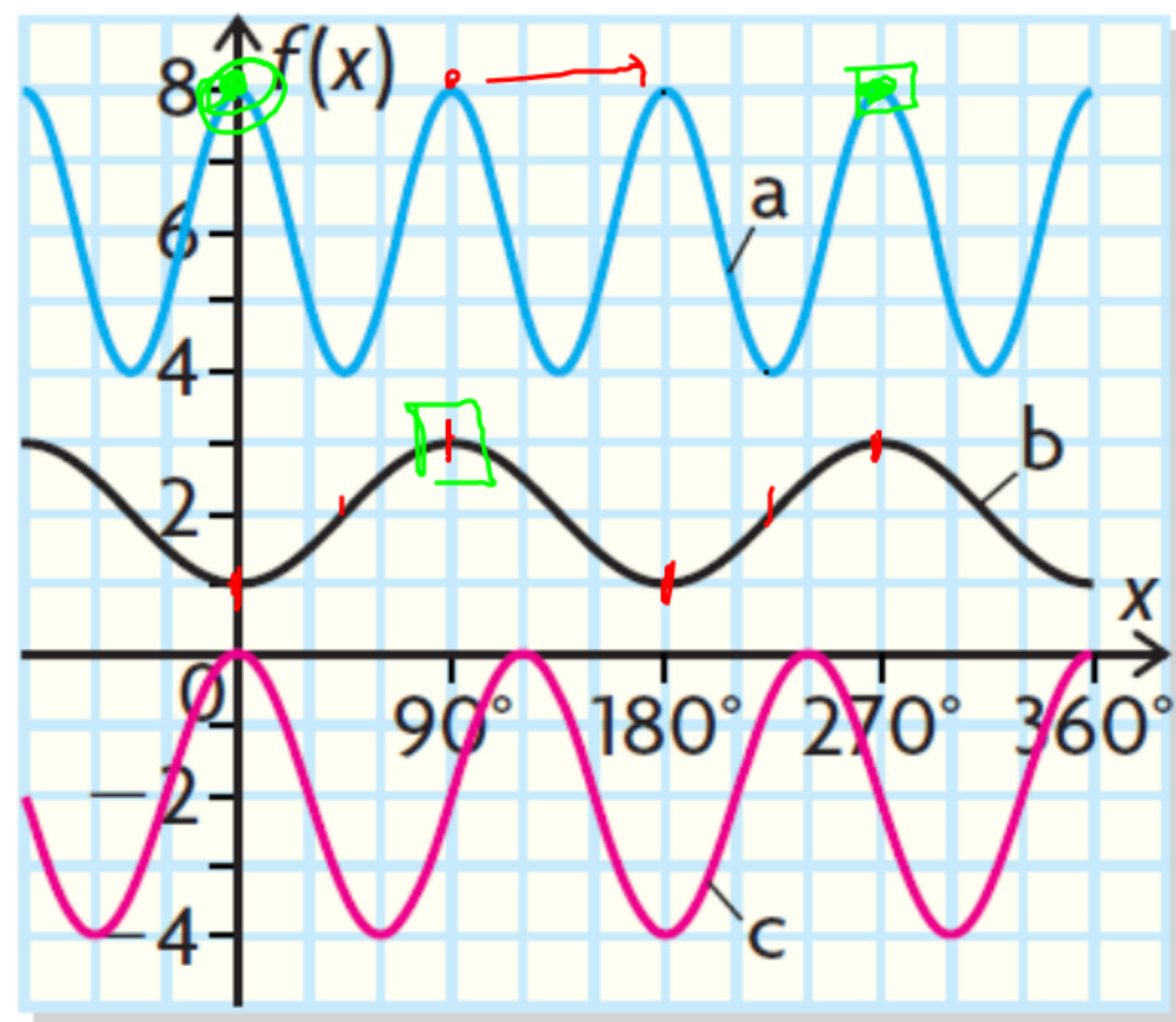
"Starts at" = y-intercept

+ $\sin(x)$ starts at 0 (middle) then goes up to the peak.

- $\sin(x)$ starts at 0 then goes down to trough

+ $\cos(x)$ starts at peak

- $\cos(x)$ starts at trough.



$$a) P = 8, T = 4 \therefore y = 6 \text{ (c)}$$

$$\text{amp} = 2 \text{ (a)}$$

$$\text{Period} = 90^\circ \therefore k = \frac{360}{90} = 4 \text{ (k)}$$

$$f(x) = 2 \cos(4(x + 0)) + 6$$

how far from
y-axis

$$b) P = 3, T = 1 \therefore y = 2 \text{ (c)}$$

$$\text{amp} = 1 \text{ (a)}$$

$$\text{Period} = 180^\circ$$

$$\therefore k = \frac{360}{180} = 2$$

$$y = -1 \cos(2(x + 0)) + 2$$

$$y = 1 \cos(2(x - 90)) + 2$$

x	0°	45°	90°	135°	180°	225°	270°
y	9	7	5	7	9	7	5

Peak = 9, Trough: 5, $y = 7$ (c)

Amp = 2 (a)

Period = 180 $\therefore k = \frac{360}{180} = 2$ (k)

$$f(x) = 2\cos(2(x + 0)) + 7$$

$$f(x) = 2\sin(2(x - 135)) + 7$$

A sinusoidal function has an amplitude of 4 units, a period of 120° , and a maximum at $(0, 9)$. Determine the equation of the function.

$$\text{amp} = 4 \quad (a)$$

$$\text{Period: } 120^\circ \quad \dots \quad k = \frac{360}{120} = 3 \quad (k)$$

$$\text{Max} = \text{Peak} = 9 \quad \dots \quad y = 5 \quad (c)$$

$$f(x) = 4 \cos(3x) + 5$$

A group of students is tracking a friend, John, who is riding a Ferris wheel. They know that John reaches the maximum height of 11 m at 10 s and then reaches the minimum height of 1 m at 55 s.

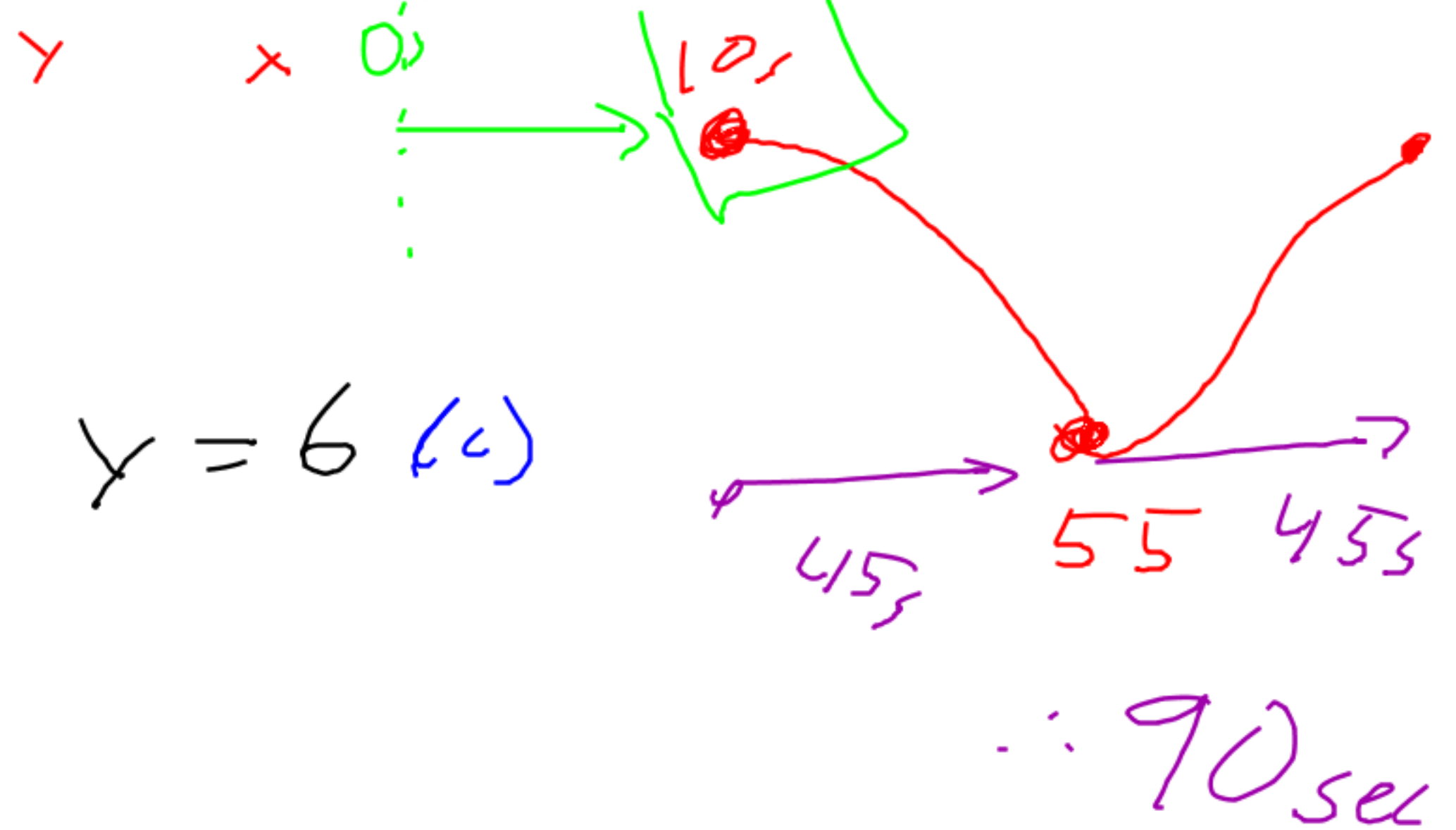
$$(10, 11) \text{ and } (55, 1)$$

$$\text{Peak} = 11, \text{ Trough} = 1 \quad \therefore y = 6 \text{ (c)}$$

$$\text{Amp} = 5 \text{ (a)}$$

$$\text{Period} = 90 \quad \therefore k: \frac{360}{90} = 4$$

$$f(x) = 5 \cos(4(x - 10)) + 6$$



How high after 2 min?

↳ 120 seconds.

$$f(120) = 5 \cos(4(120 - 10)) + 6$$

$$f(120) = 5 \cos(440) + 6$$

$$f(120) = 6.9 \text{ m}$$